# **PhD Mathematics**

Course Structure and Syllabus
(Based on Choice Based Credit System)
2016 onwards

# IK Gujral Punjab Technical University

#### VISION

To be an institution of excellence in the domain of higher technical education that serves as the fountainhead for nurturing the future leaders of technology and techno- innovation responsible for the techno-economic, social, cultural and environmental prosperity of the people of the State of Punjab, the Nation and the World

#### MISSION

- To provide seamless education through the pioneering use of technology, in partnership with industry and society with a view to promote research, discovery and entrepreneurship.
- To prepare its students to be responsible citizens of the world and the leaders of technology
  and techno-innovation of the 11st Century by developing in them the desirable knowledge,
  skills, and attitudes base for the world of work and by instilling in them a culture for
  seamlessness in all facets of life.

#### **OBJECTIVES**

- To offer globally relevant, industry-linked, research-focused, technology-enabled seamless
  education at the graduate, postgraduate and research levels in various areas of engineering
  & technology and applied sciences keeping in mind that the manpower so spawned is
  excellent in quality, is relevant to the global technological needs, is motivated to give its
  best and is committed to the growth of the Nation.
- To foster the creation of new and relevant technologies and to transfer them to industry for effective utilization.
- To participate in the planning and solving of engineering and managerial problems of relevance to global industry and to society at large by conducting basic and applied research in the areas of technologies.
- To develop and conduct continuing education programs for practicing engineers and managers with a view to update their fundamental knowledge base and problem-solving capabilities in the various areas of core competence of the University.

Scheme & Syllabus (PhD Mathematics) Batch 2016 & Onwards

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- To develop strong collaborative and cooperative links with private and public sector industries and government user departments through various avenues such as undertaking of consultancy projects, conducting of collaborative applied research projects, manpower development programs in cutting-edge areas of technology etc.
- To develop comprehensive linkages with premier academic and research institutions within the country and abroad for mutual benefit.
- To provide leadership in laboratory planning and in the development of instructional resource material in the conventional as well as in the audio-visual, the video and computer-based modes.
- To develop programs for faculty growth and development both for its own faculty as well
  as for the faculty of other engineering and technology institutions.
- To anticipate the global technological needs and to plan and prepare to cater to them.
- To interact and participate with the community/society at large with a view to inculcate in them a feel for scientific and technological thought and endeavor and
- To actively participate in the technological development of the State of Punjab through the
  undertaking of community development programs including training and education
  programs catering to the needs of the unorganized sector as well as that of the
  economically and socially weaker sections of society.

# ACADEMIC PHILOSOPHY

The philosophy of the education to be imparted at the University is to awaken the "deepest potential" of its students as holistic human beings by nurturing qualities of self-confidence, courage, integrity, maturity, versatility of mind as well as a capacity to face the challenges of tomorrow to enable them to serve humanity and its highest values in the best possible way.

# **DEPARTMENT OF MATHEMATICAL SCIENCES**

#### VISION

To be a knowledge nerve centre in Mathematical Sciences, Pure and Applied Research and industry requirements for creating sustainable infrastructure and enhancing quality of life

#### MISSION

- To offer globally-relevant, industry-linked, research-focused, technology-enabled seamless education at the graduate, postgraduate and research levels in various areas of Mathematical sciences keeping in mind that the manpower so spawned is excellent in quality, is relevant to the global scientific and technological needs, is motivated to give its best and is committed to the growth of the Nation;
- To develop and conduct continuing education programs for Science graduates with a view to update their fundamental knowledge base and problem-solving capabilities in the various areas of core specialization of the University;
- To develop comprehensive linkages with premier academic and research institutions within the country and abroad for mutual benefit.

# PhD (Mathematics) Program

The main objective of this program is to cultivate a mathematical aptitude and nurture the interests of the students towards problem solving aptitude. Further, it aims at motivating the young minds for research in mathematical sciences and to train computational scientists who can work on real life challenging problems. It further aims at motivating the students to pursue research and teaching as profession.

**Duration:** PhD Mathematics is an advance research level program of the Department of Mathematics which is 8-years (maximum) program. It is consisting of a Pre-PhD course work of one semester duration and six-monthly progress reports evaluated by RAC (Research Advisory Committee).

Program Code: MPHM (Doctor of Philosophy in Mathematics)

**Eligibility:** M.A./M.Sc. or equivalent from a recognized university with Mathematics as one of the major subjects with at least 55% marks in aggregate or its equivalent grade B in UGC 7-point scale. A relaxation of 5% or an equivalent relaxation of grade shall be allowed to SC/ST/OBC (non-creamy layer) or other categories decided by commission from time to time. The candidate must qualify PhD Entrance Exam and Interview conducted by the University. The NET/GATE qualified candidates are exempted from PhD Entrance Test.

**PROGRAM OBJECTIVES:** The Program Objectives are the knowledge skills and attributes which the students have at the time of post-graduation. At the end of the program, the student will be able to:

| PO1 | Apply the scientific knowledge of Mathematics specialization for deeper understanding of the real world phenomena.   |
|-----|--|
| PO2 | Identify, formulate, research literature, and analyze advanced scientific problems reaching substantiated conclusions using first principles of mathematics.   |
| PO3 | Design solutions for advanced scientific problems and design system components for multi-disciplinary field processes.   |
| PO4 | Use research-based knowledge and research methods including design of experiments, analysis and interpretation of results, and synthesis of the information to provide valid conclusions.  |
| PO5 | Create, select, and apply appropriate techniques, resources, and modern scientific and IT tools including prediction and modelling to complex scientific activities with an understanding of the limitations.  |
| PO6 | Apply reasoning informed by the contextual knowledge to assess societal, health, safety, legal and cultural issues and the consequent responsibilities relevant to the professional scientific practices.  |
| PO7 | Communicate effectively on complex scientific activities with the Scientific/engineering community and with society at large, such as, being able to comprehend and write effective reports and design documentation, make effective presentations, and give and receive clear instructions. |
| PO8 | Recognize the need for and have the preparation and ability to engage in independent and life-long learning in the broadest context of scientific and technological change.  |

# PROGRAM SPECIFIC OUTCOMES: At the end of the program, the student will be able to:

| PSO1 | Apply principles of advance mathematical concepts in understanding, applying and analysis of mathematical problems.                              |
|------|--|
| PSO2 | To develop human resource with specialization in theoretical and experimental techniques required for career in academia, research and industry. |
| PSO3 | To introduce advanced ideas and techniques required in emerging areas of Mathematics.  |
| PSO4 | Engage in lifelong learning and adapt to changing professional and societal needs.   |

# Scheme of the Pre PhD Course Work

# Contact Hours: 17 Hrs.

| Course Code       | Course Title                             | Course Type | Load Allocation |   |   | Marks Distribution |          |              | Credits |
|-------------------|--|-------------|-----------------|---|---|--------------------|----------|--------------|---------|
|                   |  |             | L               | Т | Р | Internal           | External | Total<br>100 | -       |
| MPHM-101          | Research Methodology                     | Compulsory  | 4               | 0 | 0 | 40                 | 60       |              | 4       |
| MPHM-102          | PHM-102 Methods in Applied Mathematics   |             | 4               | 0 | 0 | 40                 | 60       | 100          | 4       |
| MPHM-103          | Continuum Mechanics                      | 7           | 4               | 0 | 0 | 40                 | 60       | 100          | 4       |
| MPHM-104          | Advanced Analysis                        |             | 4               | 0 | 0 | 40                 | 60       | 100          | 4       |
| UC-MSM-<br>504-18 | Advanced Number Theory                   | Elective    | 4               | 0 | 0 | 40                 | 60       | 100          | 4       |
| UC-MSM-<br>510-18 | Advanced Numerical<br>Analysis           |             | 4               | 0 | 0 | 40                 | 60       | 100          | 4       |
| MPHM-105          | Presentation/Seminar                     | Compulsory  | 3               | 0 | 0 | 75                 | 0        | 75           | 3       |
| MPHM-106          | Interdisciplinary                        | Compulsory  | 4               | 0 | 0 | 40                 | 60       | 100          | 4       |
|                   | Research and Publication<br>Ethics (RPE) | Compulsory  | 2               | 0 | 0 | 20                 | 30       | 50           | 2       |
|                   | Total                                    |             | 17              | 0 | 0 | 215                | 210      | 425          | 17      |

| MPHM-1      | 01 Res       | earch Met     | hodology    |              | L-4        | , T-0, P-0    | 4 (       | Credits      |
|-------------|--------------|---------------|-------------|--------------|------------|---------------|-----------|--------------|
| Pre-requis  | ite: Stude   | nts must ha   | ve the kno  | owledge of   | basic stat | istics and ex | cel, wor  | d, LATEX     |
| software ar | nd online s  | earch engin   | nes.        |              |            |               |           |              |
| Course Ol   | ojectives:   | The object    | ive of the  | course on    | Research   | Methodol      | ogy is to | equip the    |
| PhD schola  | ers with the | e practical   | aspects of  | LATEX, N     | Mathemati  | ca and MA     | ΓLAB so   | ftware and   |
|             |              |               |             |              |            | in paper wi   |           | -            |
|             |              |               |             | irthermore.  | students   | will be in    | roduced   | to Online    |
| resources f |              |               |             |              |            |               |           |              |
| Course Ou   |              |               |             |              |            |               |           |              |
| CO1         |              |               |             |              |            | s and data s  |           |              |
| CO2         | Able to u    | ise researcl  | n methods   | in research  | literature | flow charts   | S         |              |
| CO3         | Sketch g     | raphs, drav   | v flow cha  | rts, survey  | research i | elated prob   | lems and  | l infer data |
|             |              | ıltiple disci |             |              |            |               |           |              |
| CO4         | Apply th     | ne knowled    | ge of Mul   | ltivariate a | nalysis an | d computat    | ional tec | hniques in   |
|             |              | problem ar    | -           |              |            |               |           |              |
| CO5         | Understa     | and the fund  | lamental re | elation bety | ween motiv | vation of res | search an | d Methods    |
|             | in resear    |               |             |              |            | ×             |           |              |
|             | Map          | ping of co    | urse outco  | omes with    | the progr  | am outcon     | ies       |              |
|             | PO1          | PO2           | PO3         | PO4          | PO5        | PO6           | PO7       | PO8          |
| CO1         |              |               |             | 1            | ٧          |               | ٧         |              |
| CO2         | ٧            | ٧             | ٧           | ٧            | ٧          | ٧             | ٧         | V            |
| CO3         | ٧            | ٧             | ٧           | <b>V</b>     | ٧          | ٧             | ٧         | ٧            |
| CO4         | ٧            | ٧             | ٧           | V            | ٧          | ٧             | ٧         | ٧            |
| CO5         | ٧            | ٧             | ٧           | ٧            | ٧          | ٧             | V         | ٧            |

# RESEARCH IMETHODOLOGY

# MPHM-101

- Introduction to ResearchObjectives of research, motivation in research, types of research, significance of research, research methods vs methodology, research process in flow chart, criteria of good research, problems encountered by researchers in India.
- Difference between TEX and LATEX, basics of using latex, latex input files, input file structures, layout of the document, titles, chapter and sections, cross references, foot note, environments, typesetting, building blocks of a mathematical formula, matrices, tables, including encapsulated postscript graphics, bibliography, downloading and installing LATEX packages.
- 3. Introduction to MATHEMATICA and MATLAB
- Introduction to origin, basics of importing and exporting data, working with Microsoft excel, graphing, statistics in origin, hypothesis testing, power and sample size, basic linear regression and curve fitting.
- Error Analysis and Basic Statistics Measuring errors, uncertainties, parent and sample distributions, mean and standard deviation of distribution, types of probability distribution, instrumental and statistical uncertainties, propagation of errors, specific error formulas, method of least square fitting.
- Multivariate analysis: Multiple regression, multiple discriminant analysis, multiple analysis of variance, canonical correlation analysis. Factor analysis cluster analysis, path analysis. Computational techniques.
- 7. Survey of literature: The students will be required to review literature in their respective disciplines and submit an assignment for evaluation.

#### REFERENCES:

- 1. Research methodology (http://www.newagepublishers.com/samplechapter/000896.pdf)
- 2. The not so short introduction to LATEX by TobianOetiker, Hubert Parti, HreneHyna and Elisabeth Schlegl, Version 4.16, May 08, 2005 (http://tobi.oetiker.ch/lshort/lshort.pdf)
- 3. I. Veerarajan and T. Ramachandran "Numerical methods" Tata McGraw Hill. New Delhi. 2008
- 4. Data reduction and error analysis for physical sciences by Philip R. Bevington and D.

Keith Robinson

(http://www.physast.uga.edu/files/phys3330\_fertig/BasicErrorAnalysis.pdf)

July 3/16

17/16 rmay range

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| MPHM-     | -102 M        | ethods in   | Applied M   | lathemati    | es L-4,      | T-0, P-0    | 4 C        | redits      |
|-----------|---------------|-------------|-------------|--------------|--------------|-------------|------------|-------------|
| Pre-requ  | isite: Stude  | nts must ha | ave the bas | ic knowled   | lge of Integ | ral and Di  | fferential | equations.  |
| Course C  | bjectives:    | The object  | ive of the  | course on    | Methods i    | n Applied   | Mathem     | atics is to |
| equip the | PhD scho      | lars with   | the theore  | tical aspec  | ts of class  | ical Fredh  | olm theo   | ry, Gibbs   |
| phenomer  | na, Complex   | x Fourier 7 | Transforma  | ntion and V  | Vavelet trai | nsforms. T  | heir appli | cations in  |
| multireso | lution analy  | ysis. Furth | ermore, st  | udents wil   | ll be introd | duced to    | Hankel an  | nd Mellin   |
| transform | s and their a | application | S.          |              |              |             |            |             |
| Course O  | utcomes: A    | At the end  | of the cour | se, the stud | lent will be | able to     |            |             |
| CO1       | explain t     | he differen | t types of  | Differentia  | l and Integr | ral Equatio | ons.       |             |
| CO2       | visualize     | wavelets    | and gene    | ral constru  | iction of v  | vavelets u  | sing com   | putational  |
|           | techniqu      | es.         |             |              |              |             |            |             |
| CO3       | apply the     | knowledg    | ge of Gibbs | Phenomer     | na and Stor  | mberg wa    | velet.     |             |
| CO4       | explain t     | he betweer  | n wavelet t | ransform a   | nd Fourier   | transform.  | 3          |             |
| CO5       | study fu      | rther the 1 | periodic w  | avelets, cl  | lassical Fre | edholm th   | eory and   | Complex     |
|           | Fourier i     | ntegral.    |             |              |              |             |            |             |
|           | Мар           | ping of co  | urse outco  | mes with     | the mucane   |             |            |             |
|           |               |             |             |              | the progra   | m outcon    | ies        |             |
|           | PO1           | PO2         | PO3         | PO4          | PO5          | PO6         | PO7        | PO8         |
| CO1       | PO1           | PO2<br>√    | PO3 √       |              |              |             |            | PO8         |
| CO1       |               |             |             |              | PO5          |             | PO7        | PO8         |
|           | <b>V</b>      | V           | √           | PO4<br>√     | PO5 \(       |             | PO7 √      | PO8         |
| CO2       | √<br>√        | √<br>√      | 7           | PO4 √ √      | PO5 \(       |             | PO7 √      | PO8         |

#### MPHM-102 Methods in Applied Mathematics

#### UNIT-I

Integral Equations: Their origin and classification, Relation between differential and Integral equations, IVP AND BVP reducible to Integral equations, Integral equation with separable kernals. Method of successive approximations, Classical Fredolm theory.

#### UNIT-II

Fourier series and its convergence, Gibbs phenomenon, Integration and Differentiation of Fourier Series, the phase angle form of Fourier series, Complex Fourier series and frequency spectrum. Fourier Integrals, Fourier Cosine and sine Integrals, Complex Fourier Integrals.

#### UNIT-III

Fourier transforms Properties of Fourier Transform and its Applications, Convolution, Fourier cosine and Sine transforms, Discrete Fourier Transforms, Fast Fourier Transform, Solution of equations, Hankel and Mellin transforms and their Applications.

#### UNIT-IV

Wavelets: History of wavelets, The Haar wavelets, The Stromberg Wavelet, Wavelet expansion, Multiresolution analysis with Haar wavelets, Periodic wavelets, General Construction of wavelets, Wavelet transform versus Fourier transform.

#### Suggested Readings/ Books:

- 1. Ram P. Kanwal: Linear Integral Equations. Academic Press (1971)
- Abdul J. Jerri: Introduction to Integral Equations with Applications. Monographs and Text Books in Pure and Applied Mathematics. Marcel Dekker. INC (1985)
- 3. FB Hildebrand: Methods of Applied Mathematics, Dover Publication (1965)
- Lokenath Debnath and Dambaru Bhatta: Integral Transforms and Their Applications. Second Edition Chapman and Hall/ CRC (2006)
- 5. Brian Davies: Integral Transforms and Their Applications, Text Book in Applied Mathematics, Vol 41, 3rd Edition, Springer (2002)
- P. Wojtaszczyk. A Mathematical Introduction to wavelets. London Mathematical Society Students Text. 73. (1999)
- 7. Veronique Delouille: An Introduction to Wavelet Analysis, Connexions, (2009)
- 8. Willard Miller. Introduction to the Mathematics of Wavelets, University of Minnesota. (2006)
- 9. Peter V. O'Neil. Advanced Engineering Mathematics, Thomson.

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remay remark.

| МРНМ-      | 103                  | Contin   | uum Mec     | hanics       | L-4          | , T-0, P-0                  | 4 C        | redits                 |  |  |
|------------|----------------------|--|-------------|--------------|--------------|-----------------------------|------------|------------------------|--|--|
| Pre-requi  | site: Stude          | nts must ha  | ave the bas | sic knowled  | dge of Mas   | ss, density, l              | aws of m   | otion and              |  |  |
| Course O   | lars with th         | e theoretic  | al aspects  | of continu   | um mecha     | um Mechan                   | strain, ec | <sub>l</sub> uilibriur |  |  |
| viscous fl |                      | . Furtherm   |             |              |              | nd boundary<br>red to Entre |            |                        |  |  |
| Course O   | utcomes: A           | At the end of  | of the cour | se, the stud | dent will be | e able to                   |            |                        |  |  |
| COI        |                      | the basic clasticity, sh   |             |              | 37865        | on, spatial                 | coordinat  | es, stress             |  |  |
| CO2        | apply the            | knowledg   | e of stress | analysis to  | homogen      | ous isotrop                 | ic bodies. |                        |  |  |
| CO3        |                      | use programming in plotting and visualization of graphs of action of surface forces on fluids. |             |              |              |                             |            |                        |  |  |
| CO4        | obtain go            | overning ec  | uations fo  | r a viscous  | fluid flow   | /.                          |            |                        |  |  |
| CO5        | study fur<br>motion. | rther the ba   | alance of   | energy, en   | tropy ineq   | uality and                  | Euler's eq | uation o               |  |  |
|            | Мар                  | ping of co   | urse outco  | mes with     | the progr    | am outcom                   | ies        |                        |  |  |
|            | PO1                  | PO2  | PO3         | PO4          | PO5          | PO6                         | PO7        | PO8                    |  |  |
| CO1        | V                    | <b>V</b>   | √           | <b>√</b>     | √            |                             | √          |                        |  |  |
| CO2        | <b>V</b>             | √  | V           | √            | √            |                             | <b>√</b>   |                        |  |  |
| CO3        | √                    | V  | <b>V</b>    | √            | √            | √                           | √          | V                      |  |  |
| CO4        | √                    | <b>√</b>   | √           | <b>√</b>     | √            |                             | <b>√</b>   |                        |  |  |
| CO5        |                      |  | NV.         |              |              |                             |            |                        |  |  |

#### MPHM 102 Continuum Mechanics

#### Unit-I

Continuum Hypothesis: Notion of Continuum. Configuration of a Continuum. Mass and Density, Description of motion, Material and Spatial Coordinates

Affine Infinitesimal Affine Transformation. Geometrical Interpretation of the Components of Strain, Strain Quadric of Cauchy, Principal Strains, Invariants, General Infinitesimal Deformation, Examples of strain, Notation, Equations of Compatibility. Finite Deformation

# Unit-II

Analysis of Stress: Body and Surface Forces, Stress Tensor, Note on Notation and Units, Equations of Equilibrium, Transformation of Coordinates, Stress Quadric of Cauchy, Maximal Normal and Shear Stresses, Examples of Stresses

Stress Strain Relations: Hookes law, Generalized Hookes law, Homogeneous isotropic bodies. Elastice moduli of isotropic bodies. Equilibrium Equations for an isotropic elastic solid. Dynamical equations of an isotropic elastic solid.

#### Unit-III

The strain energy function and its connection with Hooke's law. Uniqueness of solution of

Boundary-value problems of Elasticity, Saint-Venant's Principle.

Fundamental laws of continuum mechanics: Conservation of mass. Balance of linear momentum, Balance of angular momentum, General solutions of the Equation of Equilibrium. Balance of energy. Entropy inequality, Constitutive Equations

Equations of fluid mechanics: Viscous and non-Viscous fluids. Stress tensor for a non-viscous fluid. Governing Equations for a non-viscous fluid flow, Initial and boundary conditions, Euler's equation of motion. Equation of motion of an elastic fluid. Stress tensor for a viscous fluid. Shear viscosity and bulk viscosity. Governing equation for a viscous fluid flow. Initial and boundary conditions. Navier- Stokes equation.

# Suggested Readings/ Books:

- 1. Sokolnikoff, I.S., Mathematical Theory of Elasticity, Krieger Publishing Company (1983).
- Chandrasekharaiah and Debnath, Continuum Mechanics, Academic Press (1994).
- 3. Jog. C. S., Foundations and Applications of Mechanics: Volume 1: Continuum Mechanics. Norosa Publications, (2006).

fourther may remarks

| MPHM-10      | )4   | Adva   | nced Ana    | lysis        | L-4          | , T-0, P-0   | 4 C          | redits     |  |  |
|--------------|--|--|-------------|--------------|--------------|--------------|--------------|------------|--|--|
| Pre-requisi  | te: Studen   | nts must ha  | ive the bas | ic knowled   | lge of Four  | ier Transfo  | rmation,     | compact    |  |  |
| space and v  | ariational   | problems.  |             |              |              |              |              |            |  |  |
| Course Ob    | jectives: '  | The object   | ive of the  | course on    | Advanced     | Analysis     | is to equip  | the PhD    |  |  |
| scholars wi  | th the the   | coretical as   | spects of t | est function | ons and the  | eir distribu | tions, trac  | e theory.  |  |  |
| Elliptic bou | ındary va  | lue proble   | ms and e    | igen value   | problems     | . Their ap   | plications   | in weak    |  |  |
| solutions of | elliptic b   | ooundary v   | value prob  | lems. Furt   | hermore, s   | tudents wi   | ll be intro  | oduced to  |  |  |
| Galerkin me  | thod and   | finite elem  | ent metho   | ds.          |              |              |              |            |  |  |
| Course Out   | tcomes: A  | at the end o   | of the cour | se, the stuc | lent will be | able to      |              |            |  |  |
| CO1          | understar  | nd and de  | scribe the  | different    | concepts     | of Schwart   | z space,     | tempered   |  |  |
|              | distributi   | ons, and fi  | nite eleme  | nt methods   | S.           |              |              |            |  |  |
| CO2          | obtain the   | obtain the weak solutions of elliptic boundary value problems. |             |              |              |              |              |            |  |  |
| CO3          | analyze operations with distributions and trace theory.                    |  |             |              |              |              |              |            |  |  |
| CO4          | understand Galerkin method and maximum principles in eigen value problems. |  |             |              |              |              |              |            |  |  |
| CO5          | have a so  | lid founda   | tion in fun | damentals    | required to  | solve ellip  | tic bound    | lary value |  |  |
|              | problems   |  |             |              |              |              |              |            |  |  |
|              | Map  | ping of co   | urse outco  | mes with     | the progra   | am outcom    | es           |            |  |  |
|              | PO1  | PO2  | PO3         | PO4          | PO5          | PO6          | PO7          | PO8        |  |  |
| CO1          | $\sqrt{}$  | √  | V           | √ <b>.</b>   |              | V            | $\checkmark$ | V          |  |  |
| CO2          | $\checkmark$   | <b>√</b>   | √           | √            |              | V            | $\sqrt{}$    | V          |  |  |
| CO3          | $\checkmark$   | √  | <b>V</b>    | <b>V</b>     | 27           | √            | √            | V          |  |  |
| CO4          | $\checkmark$   | <b>V</b>   | V           | <b>V</b>     |              | √            | $\checkmark$ | V          |  |  |
| CO5          |  | and a  | a)          | -1           | *            | 2/           | J            | al.        |  |  |

# Advanced Analysis

#### Unit-I

Distributions: Test functions & Distributions, Some Operations with Distributions, Supports and Singular Supports of Distributions, Convolution of functions, Convolution of Distributions, Fundamental solutions, The Fourier Transform, The Schwartz Space, The Fourier Inversion formula, Tempered Distributions.

#### Unit-II

Sobolev spaces: Definition and basic properties, Approximation by smooth functions, Extension theorems, Imbedding theorems, compactness theorem, Dual spaces, fractional order spaces, trace spaces, trace theory

#### Unit-III

Weak solutions of elliptic boundary value problems: Some abstract variational problems, examples of elliptic boundary value problems, Regularity of weak solutions, Examples of Galerkin method, Maximum Principles, eigen value problems, Introduction to Finite element methods.

# Reference Book:

S Kesavan: Topic in Functional Analysis and Applications, New Age Publishers (P) Limited; 2003.

Chapter-1, 2 and 3.

|           | -MSM-<br>04-18           |          | Advanced     | l Number     | Theory       | L-4, T         | T-0, P-0    | 4 Cre      | dits      |
|-----------|--------------------------|----------|--------------|--------------|--------------|----------------|-------------|------------|-----------|
| Pre-r     | equisite:                | Eleme    | entary Nun   | nber Theor   | У            |                |             |            |           |
| Cour      | se Object                | ives:    | This Cour    | se helps th  | e students   | to underst     | and the co  | ncept of F | Partition |
|           |                          |          |              | e we introd  |              |                |             |            |           |
|           |                          |          |              | -Gordon id   |              |                |             | •          |           |
|           | partitions<br>tant theor |          | their app    | lications.   | Also, the    | weak and       | strong v    | ersions of | variou    |
|           |                          |          | t the and    | of the cour  | co the stud  | lant will b    | a abla ta   |            |           |
| Jours     | se Outcor                | iies. A  | ti the end ( | or the cour  | se, the stuc | ient win bi    | e able to   |            |           |
| CO1       | understa                 | nd the   | different    | types of pa  | artitions &  | compositi      | ons.        |            |           |
| CO2       | students                 | 11:11 h  | ANTIO O THOM | king know    | ladge of th  | a riani arra 1 | rmas afid   |            |           |
| 202       | students                 | WIII II  | iave a wor   | king know    | reage of th  | ie various i   | ypes of ide | entities   |           |
| CO3       | work wi                  | th con   | igruence's   | , solve cor  | igruence e   | quations ar    | nd systems  | of equati  | ons wi    |
|           | one and                  | more     | variables.   |              |              |                |             |            |           |
| CO4       | be litera                | te in th | ne languag   | e and nota   | tion of nur  | nber theor     | V.          |            |           |
| 1998 SA U |                          |          |              |              |              | =              | X.20        |            |           |
| 05        | understa                 | nd the   | e concept of | of for n-col | or partition | ns             |             |            |           |
|           |                          | Марр     | oing of cou  | irse outco   | mes with t   | he progra      | m outcom    | ies        |           |
|           |                          | O1       | PO2          | PO3          | PO4          | PO5            | PO6         | PO7        | PO8       |
| CO        | 1                        | √        | $\checkmark$ | <b>√</b>     | <b>√</b>     |                | <b>√</b>    | √          | √         |
| CO        | 2                        | V        | V            | V            | √            |                | ~           | √          | √         |
| CO        | 3                        | V        | V            | V            | V            |                | <b>V</b>    | √          | √         |
| CO        | 4                        | <b>V</b> | V            | V            | <b>√</b>     | √              | √           | √          | √         |
|           |                          |          |              |              |              |                |             |            |           |

# Course Title: Advanced Number Theory Course Code: UC-MSM-504-18

#### UNIT-I

Partitions, Compositions, Ferrers graphs, Jacobi's triple product identity, Congruence properties of p(n), Rogers-Ramanujan identities, Basic hypergeometric series, q-binomial theorem, Sylvester's theorem (Statement only), Heine's transformation (Statement only).

#### **UNIT-II**

Restricted partitions, q-Gauss theorem, Gaussian polynomials, Bailey's lemma (weak version) (Statement only), Rogers lemma, q-Saalschutz's theorem (Statement only), Finite version of q-Saalschutz's theorem.

#### UNIT-III

Schur's theorem, Gollnitz-Gordon identities, Generalization and various analogues of Rogers-Ramanujan identities, Bailey's lemma (strong version) (Statement only), Watson's q-analogue of Whipple's theorem (Statement only) and its applications in deriving Rogers-Ramanujan identities and Gollnitz-Gordon identities.

#### **UNIT-IV**

Rank & Crank of a partition, n-colour partitions, Conjugate and self-conjugate n-colour partitions, Restricted n-colour partitions, Rogers-Ramanujan type identities for n-colour partitions.

# RECOMMENDED BOOKS:

- 1. Agarwal, A.K., Padmavathamma and Subbarao, M.V., *Partition Theory*, Atma Ram & Sons, Chandigarh, 2005.
- 2. Andrews, G.E., *The Theory of Partitions, Encyclopedia of Mathematics and its Applications* (Addison-Wesley), 1976, Re-issued: Cambridge University Press, Cambridge, 1988.
- 3. Gasper, G. and Rahman, M., *Basic Hypergeometric Series, Encyclopedia of Mathematics and its Applications*, Vol. 35, Cambridge University Press, Cambridge, 1990.
- 4. Agarwal, R.P., Resonance of Ramanujan Mathematics, Vol. 1 (New Age International), 1996.
- 5. Gupta, H., Selected Topics in Number Theory, ABACUS Press, 1980.
- 6. N.J. Fine, *Basic Hypergeometric Series and Applications*, Mathematical Surveys and Monographs, No. 27, American Mathematical Society, 1988.

| UC-MSI<br>510-18                        |   | Advance  | d Numerio  | cal Metho  | ds  | L-4, T-0, P  | -0                                    | 4 Credits   |
|---|---|--|--|--|---|--|---------------------------------------|---|
| Pre-requis                              | ite: Basic  | c Calculus a   | and analys   | is. Basic n  | umerical a  | nalysis  |                                       |   |
| of advance<br>eigenvalue<br>application | ed numeri<br>s problem<br>s, for exam<br>nt, analys<br>of these n | cal method<br>ns, ordinary<br>mple in science<br>is and implementhods. | ds for soly<br>y and par<br>ence, engine<br>ementation | ving differ<br>tial difference<br>neering, ar<br>n of nume | rent types<br>ential equ<br>nd econom<br>rical meth | of problen<br>ations arisin<br>ics etc. The<br>ods keeping | ns viz. lin<br>ng in var<br>major foo | nd application<br>near systems,<br>rious field of<br>cus will be on<br>advantages & |
| CO1                                     | problem   | ns viz. linea  | r systems,<br>various fi                               | eigenvalu  | es probler  | ns, ordinary   | and parti                             | erent types of<br>al differential<br>e, engineering                                 |
| CO2                                     | Underst   | and advant   | ages and l   | imitations   | of advance  | ed numerica  | l methods                             | <b>*</b> .:   |
| CO3                                     |   | nd implem<br>in mind na  |  |  | ımerical n  | nethod for se  | olving a g                            | iven problem  |
| CO4                                     |   | oretical bas   |  | methods i  | n order to  | study their  | counterpa                             | rts existing in   |
| CO5                                     | deal wit  | h analytica  | lly) and fir   | nd their ap  | propriate s   |  | curately ar                           | re difficult to<br>and efficiently.   |
|   | 141   | apping or o  | course out   | comes wi   | in the pro  | grain outco  | ines                                  |   |
|   | PO1   | PO2  | PO3  | PO4  | PO5   | PO6  | PO7                                   | PO8   |
| CO1                                     | ~   | √  | <b>V</b>   | √  | √   | √  | $\checkmark$                          | $\sqrt{}$   |
| CO2                                     | <b>√</b>  | <b>√</b>   | <b>V</b>   | <b>V</b>   | √   | V  | $\checkmark$                          | $\checkmark$  |
| CO3                                     | <b>√</b>  | <b>V</b>   | <b>V</b>   | <b>√</b>   | <b>√</b>  | V  | √                                     | √   |
| CO4                                     | <b>√</b>  | <b>√</b>   | <b>V</b>   | V  | 1   | V  | √                                     | <b>V</b>  |
| CO5                                     | V   | V  | V  | V  | ~   | √  | √ ·                                   | <b>V</b>  |

# Course Title: Advanced Numerical Methods Course Code: UC-MSM-510-18

#### Unit-I

**Iterative Methods for Linear Systems & Eigenvalue problem:** The classical iterative methods: Jacobi, Gauss-Seidel and Successive Over Relaxation (SOR) methods. Conjugate gradient method. Eigenvalues & eigenvectors: Rayleigh power method & Givens method.

#### Unit-II

**Finite Difference Methods:** Explicit and implicit schemes, consistency, stability and convergence, Lax equivalence theorem, numerical solutions to elliptic, parabolic and hyperbolic partial differential equations.

#### Unit-III

**Approximate methods of solution:** Rayleigh-Ritz, collocation and Galerkin methods, properties of Galerkin approximations, Petrov-Galerkin method, Generalized Galerkin method.

#### Unit-IV

**Finite Element Method (FEM):** FEM for second order problems, One- and two-dimensional problems, The finite elements (elements with a triangular mesh and a rectangular mesh and three-dimensional finite elements), Fourth-order problems, Hermite families of elements, iso-parametric elements, numerical integration.

# BOOKS RECOMMENDED:

- 1. Jain, M.K, Iyengar, S.R.K. and Jain, R.K., *Numerical Methods for Scientific and Engineering Computation*, 5<sup>th</sup> Edition, New Age international, 2008.
- 2. Hoffman Joe D., Numerical methods for Engineers and Scientists, McGrow-Hill, 1993.
- 3. Atkinson, K.E, An Introduction to Numerical Analysis, 2nd Edition, John Wiley, 2004.
- 4. Gupta R.S., Elements of Numerical Analysis, McMillan India, 2009
- 5. Seshu P., Textbook of Finite Element Analysis, Prentice Hall India, 2003.

|           | 2   | Research   | and Publi<br>(RPE) | cation Eth   | iics        | L-4, T-0, I  | P-0     | 4 Credits    |  |  |
|-----------|---|--|--------------------|--------------|-------------|--------------|---------|--------------|--|--|
| Pre-requ  | isite: Ethic                                | al and mor   | al respons         | ibilities to | wards rese  | arch comm    | unity.  |              |  |  |
| responsib | Objectives:<br>ility toward<br>n, predatory | s the resea  | rch comm           | unity. The   |             |              |         |              |  |  |
| Course O  | outcomes: A                                 | At the end   | of the cour        | se, the stud | dent will b | e able to    |         |              |  |  |
| CO1       | familiar                                    | ize with me  | oral philos        | ophy of Ro   | esearch Et  | nics.        |         |              |  |  |
| CO2       | acquire l                                   | acquire knowledge on definition, concept and problems that lead to unethical behavior in research. |                    |              |             |              |         |              |  |  |
| CO3       | understa                                    | understand predatory publishers and journals.  |                    |              |             |              |         |              |  |  |
| CO4       | search re                                   | elevant jou  | rnals and i        | esearch pa   | pers using  | online reso  | ources. |              |  |  |
| CO5       |   |  |                    |              | -           | grity and in |         | nonesty.     |  |  |
|           |   |  |                    |              |             | gram outc    |         |              |  |  |
|           | PO1   | PO2  | PO3                | PO4          | PO5         | PO6          | PO7     | PO8          |  |  |
| CO1       | √   | V  | √                  | V            |             | <b>√</b>     | √       | $\checkmark$ |  |  |
| CO2       | √   | √  | √                  | <b>√</b>     |             | √            | √       | $\sqrt{}$    |  |  |
| CO3       | <b>√</b>                                    | V  | √                  | √            |             | <b>√</b>     | √       |              |  |  |
| CO4       | <b>√</b>                                    | √  | V                  | √            | <b>√</b>    | √            | √       |              |  |  |
| CO5       |   |  |                    |              |             |              |         |              |  |  |

# I.K. GUJRAL PUNJAB TECHNICAL UNIVERSITY

Estd. Under Punjab Technical University Act, 1996 (Punjab Act No. 1 of 1997)

Ref. No. : IKGPTU/Reg/NF/ 169

Dated: 23.06.2021

# NOTIFICATION

Sub: Introduction of two credit course "Research and Publication Ethics (RPE).

I.K. Gujral Pujnab Technical University, Jalandhar has introduced a mandatory two credit course on "Research and Publication Ethics (RPE) for all Ph.D students in their pre-registration course work from January 2021 onwards. The course content/ structure as per UGC guidelines (letter No.D.O.No.F.1-1/2018 (Journal/CARE) dated December 2019) has been included in Ph.D. course work. The details are as follows:

# Research and Publication Ethics (RPE) (2 Credits)

#### 1. Course structure

 The course comprises of six modules listed in table below. Each module has 4-5 units.

| Modules  | Unit title                    | Teaching hours |  |
|----------|-------------------------------|----------------|--|
| Theory   |                               |                |  |
| RPE 01   | Philosophy and Ethics         | 4              |  |
| RPE 02   | Scientific Conduct            | 4              |  |
| RPE 03   | Publication Ethics            | 7              |  |
| Practice |                               |                |  |
| RPE 04   | Open Access Publishing        | 4              |  |
| RPE 05   | Publication Misconduct        | 4              |  |
| RPE 06   | Database and Research Metrics | 7              |  |
|          | Total                         | 30             |  |

Syllabus (as suggested by UGC)

Sm

I. K. Gujral Punjab Technical University, Jalandhar

Jalandhar Kapurthala Highway, Near Pushpa Gujral Science City, Kapurthala - 144 603

Ph. No. 01822 - 282521, 282501, Email: registrar@ptu.ac.in

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### THEORY

# · RPE 01: PHILOSOPHY AND ETHICS (3hrs.)

- 1. Introduction to Philosophy: definition, nature and scope, concept, branches
- 2. Ethics: definition, moral Philosophy, nature of moral judgements and reactions

# RPE 02: SCIENTIFIC CONDUCT (5hrs.)

- 1. Ethics with respect to science and research
- 2. Intellectual honesty and research integrity
- 3. Scientific misconducts: Falsification, Fabrication and Plagiarism (FFP)
- 4. Redundant publications: duplicate and overlapping publications, salami slicing.
- 5. Selective reporting and misrepresentation of data

# RPE 03: PUBLICATION ETHICS (7hrs.)

- 1. Publication Ethics: definition, introduction, and importance
- 2. Best practices/standards setting initiatives and guidelines: COPE, WAME, etc.
- 3. Conflicts of interest
- Publication misconduct: definition, concept, problems that lead to unethical behaviour and vice versa, types.
- 5. Violation of publication ethics, authorship, and contributorship
- 6. Identification of publication misconduct, complaints and appeals
- 7. Predatory publishers and journals

#### **PRACTICE**

### RPE 04: OPEN ACCESS PUBLISHING (4hrs.)

- 1. Open access publications and initiatives
- SHERPA/RoMEO online resource to check publisher copyright & self-archiving policies.
- 3. Software tool to identify predatory publications developed by SPPU.
- 4. Journal finder/journal suggestion tool viz. JANE, Elsevier Journal Finder, Springer Journal Suggester, etc.

# RPE 05: PUBLICATION MISCONDUCT (4hrs.)

# A. Group Discussion (2hrs.)

- 1. Subject specific ethical issues, FFP, authorship
- 2. Conflicts of interest
- 3. Complaints and appeals: examples and fraud from India and abroad

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# B. Software tools (2hrs.)

Use of plagiarism software like Turnitin, Urkund, and other open-source software tools.

# RPE 06: DATABASES AND RESEARCH METRICS (7hrs.)

# A. Databases (4hrs.)

- 1. Indexing databases
- 2. Citation databases: Web of Science, Scopus, etc.

# B. Research Metrics (3hrs.)

- 1. Impact Factor of journal as per Citation Report, SNIP, SJR, IPP, Cite Score
- 2. Metrics: h-index, g-index, i10 index, altmetrics

### 2. Course Work Structure - 17 Credits

All candidates admitted to Ph.D programme shall be required to complete the Ph.D course work, proposed by the Supervisor keeping in view the candidate's areas of research in the University Teaching Department. Pre Ph.D course work will be **17 credits and shall be offered on regular** basis at IKGTU campus.

Structure of course work is as under:

| ir. No.  | Nature of Course                            | Name of Course                                 | Credits | Remarks  |
|--|---|--|---------|--|
| The state of the s | Core  | Research     Methodology                       | 4       | The syllabus of RM should be formulated faculty wise such as Engineering, Sciences, Management/ Humanities and Life Sciences |
|  |   | Subject Related theory paper                   | 4       | Discipline specific related to Advancements in theoretical methods for research.   |
|  |   | 3. Presentation                                | 3       | Discipline specific  |
| 2.   | Interdisciplinary                           | 4. Elective                                    | 4       | From list of Subjects from allied fields   |
| 3.   | Research and<br>Publication Ethics<br>(RPE) | 5. Research and<br>Publication<br>Ethics (RPE) | 2       | As Per UGC   |
|  | Total Minimum cr                            | edits  | 17      |  |

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do

- a. The candidate will have to clear Courses within the first two semesters as per the programme of the Department.
- b. Direct fellowship awardees or candidates registered for Ph.D. during the middle of the semester will take up course work in the following semester
- c. The syllabus for the Pre-Ph.D. course work, not covered in the ongoing PG curriculum, will be drawn by the Board of Studies or RAC subject to the approval by BoS and highest academic body of the University.
- d. An Attendance less than the mandatory 75% (including 10% attendance benefit on medical grounds) in the course work shall attract cut in the scholarship /fellowship.

# 3. Applicability:

It is decided that the 17 credit course work will be applicable to all students which are enrolled from January 2021 onwards.

Registrar

Endst. No. IKGPTU/Reg/NF/170-174

Dated: 23.06.2021

A copy is forwarded to the following officers for information please.

- 1. Vice Chancellor Secretariat: For information of Vice Chancellor
- Dean (R&D)
- 3. Director (Main Campus): To inform all Deputy Dean (Faculty), HoDs (Teaching) and In-charge, Constituent Campuses
- 4. Director/Principal, Autonomous College
- 5. Incharge (ITS): For upload of notice in the Notice Board of University website and Ph.D admissions link also.

(Sandeep Kumar Kazal) as

Registrar